MATHEMATICS 120

INTRODUCTION TO OPTIMIZATION

Text: An Introduction to Optimization, 2nd edition, by E.K.P. Chong and S. Zak.

Classical nonlinear optimization: Unconstrained and constrained problems in several variables, Jacobian and Lagrangian methods, Kuhn-Tucker conditions. Linear programming, the simplex method, duality, applications. – One quarter of multivariable calculus is a prerequisite for this course, and a linear algebra course is a prerequisite or corequisite.

TOPICS

SUGGESTED NO. OF WEEKS

Topics from multivariable calculus and linear algebra......2 (§§ 3.1-3.5, 4.1-4.5, 5.2-5.5)

> Linear transformations, eigenvalues and eigenvectors, quadratic forms, algebraic characterization of line segments and hyperplanes, convexity, polyherdal sets, the derivative matrix of a vector valued transformation of several variables, level sets and gradients, multivariable Taylor polynomials.

> Second order conditions for unconstrained relative extrema, regional constraints, equality constraints and Lagrange multipliers, inequality constraints and the Kuhn-Tucker conditions.

> Elementary examples and applications, geometric interpretation, standard forms of linear programming problems, basic solutions and their properties.

> Review of Gauss-Jordan elimination, the Simplex Algorithm and its computational form (with proofs), variants of the Simplex Method, the dual of a linear programming problem and properties of dual programming problems.