



Special Colloquium

UCR
Mathematics
Department

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"MODULI SPACES OF MANIFOLDS"

Let M be a smooth manifold, let $\text{Diff}(M)$ denote the topological group of diffeomorphisms $M \rightarrow M$, and let $\text{BDiff}(M)$ denote the *classifying space*. For any paracompact space X , there is a one-one correspondence between the set of homotopy classes $[X; \text{BDiff}(M)]$ and the set, $\text{Bun}_M(X)$, of isomorphism classes of fibre bundles $E \rightarrow X$ with fibre M . The classifying space of $\text{BDiff}(M)$ is referred to as the *moduli space of manifolds of type M* . The study of the homotopy type of these spaces occupies a central place in smooth topology.

In this talk I will discuss some contemporary approaches to studying the homotopy type of $\text{Bdiff}(M)$, for varying M . In particular I will discuss the work of Madsen and Weiss identifying the homological type of the moduli spaces of Riemann surfaces and the results of Galatius and Randal-Williams on the moduli spaces of manifolds of dimension $2n$, I will then present recent work of mine pertaining to the moduli spaces of odd dimensional manifolds, and manifolds with boundary, and will discuss connections to cobordism categories and surgery theory.

Tuesday, January 9th, 2017

Surge 284

Talk Begins @ 4:10 p.m.

Ends @ 5:00 p.m.

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